

Reflections on narrow-reef platinum mining pillar design systems as applied to a large platinum exploration feasibility project

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Synopsis

Platinum is a highly valuable resource, its safe and economic extraction is paramount. The success of platinum mining by the bord and pillar method depends heavily on a comprehensive and dependable pillar design method. Pillars need to be large enough to safely support the load and small enough to avoid loss of resources. A critical evaluation of current pillar design systems used in narrow-reef platinum mining was undertaken using practical experience from a large feasibility-stage platinum exploration project, supplemented by observations from several platinum mines in Zimbabwe. An extensive literature survey was undertaken in order to determine the current status of design systems. Through this approach, the shortcomings of current pillar design systems are highlighted. Areas are proposed for further research to obtain a better understanding on how additional factors influence pillar system stability. The exploration work highlighted how rock mass classification methods can be utilized in determining the overall strength of pillars. Current pillar design systems for narrow-reef platinum mining consider width-to-heightratio (usually with different exponents for width and height) and the strength of the pillar material. However, there are many more important factors that are not considered and which have a bearing on pillar system stability. An in-depth study of these parameters with a view to establish effective narrow- reef platinum mining pillar design systems needs to be undertaken.

Keywords

pillar design, pre-feasibility, platinum mining, hard rock, comparative

Introduction

Pillars have been used as a means of support since the early days of mining. Pillarsupported mining methods such as bord and pillar require a reliable design system for them to be successful. This paper presents an evaluation of the current hard-rock mining pillar design systems as applied to a practical large-scale narrow-reef platinum mining feasibility study. It is vital to have a dependable pillar design system for economic and sustainable mining. Using an extensive database collected from the project, the pillar strength formulae were tested and several discrepancies noted. This necessitates the establishment of more reliable pillar design systems. In narrow-reef platinum mining, large compressive stresses accompanied by geological and geotechnical factors contribute to pillar instability. A well-formulated pillar design system is required that accounts for such factors so as to minimize pillar failures.

A pillar layout design system has to consider the hangingwall, the pillar material, and the footwall as all these three work together for the success of the system. Ozbay, Ryder, and Jager (1995) describe the hangingwall in shallow hard-rock mining situations as a rock mass containing welldefined discontinuities and subjected to deadweight compression. When the hangingwall is unsupported, it becomes susceptible to backbreaks if critical spans are exceeded (Ozbay, Ryder, and Jager, 1995).

Pillar design theory

Different pillars are used in narrow-reef platinum mining, depending on the function the pillar is to serve. In hard-rock tabular mining in general, a combination of pillar types is utilized. Dave (2009) classifies these types as shaft pillars, bracket pillars, boundary pillars, water barrier pillars, barrier pillars, crown pillars, sill pillars, strike-stabilizing pillars, dip-stabilizing pillars, non-yielding pillars, yielding pillars, and crush pillars. Salamon (1983) classified these pillars into three main types –support pillars, protective pillars, and control pillars. He explains that support pillars are usually laid out systematically to offer support to the undermined ground. According to this classification, protective pillars protect surface structures and underground mining excavations or separate one mine from its neighbour, while control pillars are those laid out systematically and cut in deep-level mines to curb rockbursts by reducing energy release rates.

Current pillar design systems are based on the empirical determination of pillar design parameters. This approach relies entirely on the failure of pillars for an empirical pillar

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design curve to be calibrated. It cannot be used for mines outside the empirical range that the pillar design is intended for. Several formulae are currently in use to determine pillar strength. For the calculation of load, the tributary area theory (TAT) which applies to regular mining layouts is used. Coates' (1981) method is also used to determine pillar load for large rectangular pillars like regional pillars. Parameters currently accounted for in the design of narrow reef platinum mining pillars are strength, load, width-to-height (w/h) ratio, and pillar foundation bearing capacity. The *w/h* ratio is generally used as a first indication of pillar strength. Martin and Maybee (2000) compared extensive data collected from back-analysis and concluded that most pillars fail at a *w/h* ratio of less than 1.5, while there is a substantial increase in pillar strength at a *w/h* ratio of more than 2. Stacey and Page (1986) mention that foundation failure, rather than pillar failure, can be expected at a *w/h* ratio of more than 7, provided that the pillar and foundation material are the same. Numerical modelling tools are also utilized to aid pillar design.

Pillar load determination

Tributary area theory

Pillar stresses are normally calculated using the tributary area theory (TAT), which accounts for the full cover load. This theory is used in regular mining layouts of large lateral extent (several times greater than the mining depth) and assumes that each pillar in the layout supports an equal load to the surface. This allocates full cover load to each pillar in the layout. Pillars of the same size must be used in the regular mining layout for the TAT to be applicable. This approach appears to be operationally convenient as it leads to fixed pillar-design dimensions for any given seam material and depth. The TAT assumes that a pillar carries the full load of the overburden above the pillar itself and halfway into the surrounding roadways (Salamon and Oravecz, 1976; Salamon and Munro, 1967; Hoek and Brown, 1980; Roberts *et al.*, 2002).

The average pillar stress (APS) can be expressed as a function of extraction ratio as follows:

$$APS = \frac{\sigma_V}{1-e}$$
[1]

where σ_v is the vertical component of the virgin stress (MPa), e is the areal extraction ratio, ρ is rock density (kg/m³), g is gravitational acceleration (m/s²), h is depth below ground surface (m), and $\sigma_v = \rho gh$.

Hoek and Brown (1980) present an alternative formula for calculating APS for square pillars using the TAT. For a square pillar layout, the formula is:

$$APS = \sigma_{v} \left(1 + \frac{W_{0}}{W_{p}} \right)^{2}$$
 [2]

where σ_v is the vertical component of the virgin stress, W_0 is the excavation width (bord width), and W_p is the pillar width.

Coates' method

Coates (1981) presented his formula for load calculation after realizing that while the TAT can be utilized, it is insufficient since it does not consider geometrical and rock properties in

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its formulation. He went on to consider these parameters in the derivation of his formula. Coates (1981) admitted that his formula is only applicable in the centre of the mining area with undisturbed long rib pillars and in situations where the mine span does not exceed half the depth. Coates' formula (1981), which is applicable for calculating pillar load in deep and long mining zones, is given by:

APS =
$$\sigma_{v} \propto \left[1 + \frac{2e(1+h_{s}) - kh_{s}(1-w+w_{p}n)}{h_{s}n + 2(1-e)(1+h_{s}) + \frac{2eb(1-w)}{\pi}} \right]$$
 [3]

$$e = \frac{B_o}{B_{o+B_P}}, \quad k = \frac{\sigma_h}{\sigma_v}, \quad w = \frac{\upsilon}{1-\upsilon}, \quad w_p = \frac{\upsilon_p}{1-\upsilon_p},$$
$$n = \frac{E(1-\upsilon_p^2)}{E_p(1-\upsilon^2)}, \quad b = \frac{B_P}{L}, \quad h_s = \frac{H}{L}$$

where σ_v is the vertical component of the virgin stress (MPa), e is the areal extraction ratio, H is height of the stope (m), σ_h is the horizontal component of the virgin stress (MPa), v is Poisson's ratio for abutments, v_p is Poisson's ratio for pillars, E is Young's modulus for abutments, E_p is Young's modulus for pillars, B_o is room width (m), B_p is pillar width (m), and L is width of extraction span (m).

It is evident that the formulation of Coates (1981) does not consider overburden stiffness and seam stiffness, factors that play a pivotal role in determining pillar load.

Note: Coates' method reduces to the usual TAT when L \rightarrow ∞ as shown in the calculation below.

When $L \rightarrow \infty$, $B_p = 0$, b = 0 and $h_s = 0$ such that

$$APS = \sigma_{v} \times \left[1 + \frac{2e(1+h_{s}) - kh_{s}(1 - w + w_{p}n)}{h_{s}n + 2(1-e)(1+h_{s}) + \frac{2eb(1-w)}{\pi}} \right]$$
$$APS = \sigma_{v} \times \left[1 + \frac{2e(1+0) - 0}{0 + 2(1-e)(1+0) + 0} \right] = \sigma_{v} \times \left(1 + \frac{2e}{2-2e} \right) = \sigma_{v} \left(\frac{2-2e+2e}{2-2e} \right)$$
$$= \sigma_{v} \left[\frac{2}{2(1-e)} \right] = \frac{\sigma_{v}}{1-e}$$

Coates (1981) mentions that his formula considers the following geometrical (layout) and rock characteristics: the span of the mining zone with respect to its depth, height of the pillars, pillar locations within the mining zone, horizontal stress, and modulus of deformation of the pillar and wall rock materials.

Theory of pillar strength determination

There are a number of issues that the current formulae used to determine hard-rock pillar strength do not address. Most of the strength formulae developed for hard-rock pillars have an empirical base. They were proposed after studies from different mines using failed pillar information. The formulae take the power form or linear form, but have a common aspect of considering the *w*/*h* ratio of the pillars under study. The forms of the pillar strength formulae are as given in Equations [4] and [5].

Power
$$\sigma_s = K w^{\alpha} / h^{\beta}$$
 [4]

Linear
$$\sigma_s = K \left(A + B \frac{w}{h} \right)$$
 [5]

where

 σ_s is the strength of a pillar with width *w* and height *h* K is the adjusted or non-adjusted strength of a unit cube of pillar rock determined statistically or through the use of laboratory results

 $\alpha,\,\beta,\,A,$ and B are constants.

There are several representative coal pillar strength formulae from which the currently used hard-rock pillar strength formulae were deduced. These are:

Holland and Gaddy (1956)
$$\sigma_s = K \sqrt{w}/h$$
 [6]

Holland (1964) $\sigma_s = K \sqrt{w/h}$ [7]

Salamon and Munro (1967)
$$\sigma_s = K w^{0.46} / h^{0.66}$$
 [8]

^{*}Bunschinger (1876)
$$\sigma_s = K \left(0.778 + 0.222 \frac{w}{h} \right)$$
 [9]

Bunting (1911)
$$\sigma_s = 1000 \left(0.70 + 0.30 \frac{w}{h} \right)$$
 [10]

Bieniawski (1968)
$$\sigma_s = K \left(0.64 + 0.36 \frac{w}{h} \right)$$
 [11]

While there are a lot of factors to consider in calculating pillar strength, the rock mass strength of the pillar material and the shape and the size of the pillar are the three factors which several researchers, including Salamon and Munro (1967), Wagner (1980), Stacey and Page (1986), and Madden (1990) put forward as the factors on which the pillar strength depends. They mention that width and height, and gross structural features such as clay bands, faults, and joints are the parameters that define pillar shape and size. Martin and Maybee (2000) propose that formulae developed empirically should not be used for w/h ratios of more than 2.

Hard-rock pillar strength formulae

Table I presents some strength formulae used in hard-rock pillar design.

Reflections on the practical application of the pillar design systems to a large-scale feasibility-stage platinum exploration project: some lessons

The geotechnical work undertaken by the authors for the exploration project gives an insight into areas that require attention if we are to come up with reasonably reliable pillar design parameters. It suffices to say that the quality of input into the pillar design system influences the quality of the results from it. The geotechnical work discussed in this section includes oriented core drilling, logging practice, core sampling procedure, laboratory tests, and rock mass classifications. Pillar design results for the project using different hard-rock pillar design formulae are also discussed.

Oriented core drilling

To get a true picture of the *in situ* rock, core is oriented. Core orientation involves the determination of the topmost or bottommost point of the top face of a drill run, which is then linked to the next run. The geotechnical holes were drilled using an automatic temperature control (ATC) orientation tool. In this way, an orientation line was drawn along the top of the core. This makes it easier to uniquely orient the core in space. This reference line is used to determine the trend and plunge of the joints. Several exploration boreholes were drilled on the site. These are shown in Figure 1. For this discussion, the authors chose borehole BO53A for illustrative purposes.

*Cited in Du et al. (2008)

Table I		
Hard-rock pillar strength formulae		
Researchers	Formula	Database used
Hedley and Grant (1972)	$\sigma_{\rm s} = 133 \frac{w^{0.5}}{h^{0.75}} $ [12]	Eliot Lake uranium mines, Canada.
Potvin, Hudyma, and Miller (1989)	$\frac{\sigma_s}{ucs} = 0.4162 \frac{w}{h} $ [13]	Canadian open stope mines.
Von Kimmelmann, Hyde, and Madgwick (1984)	$\sigma_{\rm s} = 65 \frac{w^{0.46}}{h^{0.66}} $ [14]	Selebi Phikwe mines, Botswana.
Sjoberg (1992)	$\sigma_s = \sigma_1 \left(0.78 + 0.22 \frac{w}{h} \right) \qquad [15]$	Zinkgruvan mine, Sweeden.
Krauland and Soder (1987)	$\sigma_{\rm s} = \sigma_1 \left(0.78 + 0.22 \frac{w}{h} \right) \qquad [16]$	Black Angel mine, Greenland.
Lunder and Pakalnis (1997)	$\sigma_{ps} = (K * UCS) * (C1 + C2 * kappa) $ [17]	Combination of databases from other authors.
Watson et al. (2008) (linear formula)	$PS = 147 \left[0.70 + 0.3 \frac{w_e}{h_e} \right] [18]$	Impala Platinum, South Africa.
Watson et al. (2008) (power formula)	Strength = $86 \frac{w_e^{0.76}}{h_e^{0.36}}$ [19]	Impala Platinum, South Africa

Notes: UCS is pillar material unconfined compressive strength, σ_1 is the strength of a pillar with a *w/h* ratio of 1, *K* is rock mass strength size factor with Lunder and Pakalnis average at 44%, Cl and C2 are empirical constants determined to be 0.68 and 0.52 respectively, and kappa is the mine pillar friction term.



Figure 1-Exploration boreholes used in the study

Downhole survey

Downhole surveying was carried out using a high-precision downhole survey instrument to identify any deviations from the planned drilling axis. The downhole survey plan and section of borehole BO53A are presented in Figure 2. No deviation from the drilling axis was identified. The deviation in the top portion of the hole was due to casing interference and is not an indication of true deviation. The high-precision instrument helps to prevent human error once set appropriately. The lack of deviation is advantageous since oriented core is recovered along the required drilling axis.

Logging practice

After core has been oriented it is then logged to determine the geotechnical parameters influencing pillar design. The logging process adopted at the exploration site is presented in Figure 3.

A total of 50 boreholes were geotechnically logged, some of which were oriented (BO53A, BO54A, BO55A, and BO61A). The oriented boreholes are used in this discussion as they capture much more geotechnical detail of the rock mass compared to the unoriented boreholes. BO53A is used for illustrative purposes in this paper. The logging was done in three stages. Three-metre runs were used for the assessment. Although geotechnical assessments were done throughout each drill-hole, the main zone of interest is the reef horizon and immediate hangingwall and footwall. As such, these are the areas presented in this discussion to maintain brevity and clarity.

Quick log per run - Log 1

Log 1 was a quick log per run, capturing rock type, total core recovery (TCR), solid core recovery (SCR), rock quality designation (RQD), as well as photographs and short comments for each run. Total core recovery is the sum of all measurable core recovered in one drill run, while SCR is defined as the sum of all sections of the core run that are greater than one core diameter. Sections of core with multiple mechanical breaks and handling breaks need to be considered as solid core. RQD is the ratio of the core recovered, counting pieces longer than 100 mm, to the total length of the run, expressed as a percentage. It is imperative to note that breakages due to handling and drilling have to be ignored and the core considered as being continuous at these points when calculating RQD. There has to be a guideline that enables the logger to pick these mechanical breaks. RQD is used for qualitative analysis of rock strength. Weak rock types like kimberlite may have low joint counts and thus record a high RQD. This RQD, when used in rock mass classification, gives an unrepresentative high value. Due to this, rock samples are sent to the laboratory for quantitative rock mass strength analysis.

Major structures - Log 2

At this stage all major structures that have a bearing on the rock mass quality are logged and evaluated. The structures include shear zones, fracture zones, faults, fractures, joints, striation lineations, fold axes, veins, and dykes. Also logged at this stage are typical orientations and brittleness properties of these structures. Water staining properties of the discontinuities are recorded. When water pressure is present in a rock mass, the surfaces of the discontinuities are forced apart and the normal stress on the discontinuity is reduced. This in turn reduces the shear strength of the discontinuities. For the typical orientations, angles α and β were measured using a



Figure 2-Downhole survey plan and section of borehole BO53A



Figure 3-Logging process adopted at the exploration site

graduated strip and a carpenter's angle. The SRK Geotechnical Core Logging Manual (2006) was used as a guide. The alpha angle (α) is the maximum dip (α) of the feature relative to the core axis, as measured by the carpenter's angle. For the beta angle (β), the plastic calibrated strip is placed with the zero on the orientation line of the same piece of core and the tape is wrapped clockwise around the core so that the 360° point returns to the orientation line. The angle (β) is then measured, clockwise, to the bottom of the ellipse. In this convention, only the upper part of the feature is used for the measurement. The measured angles are as illustrated in Figure 4.

Error concerns in logging of major structures

It is often a challenge to determine whether a discontinuity represents an open joint or a cemented joint. For this reason, it is rational to consider a cemented joint that is open in the core as an open joint fracture, since the joint is weak, hence it easily opens up. Joint infill type has an influence on the strength of joints, so experience is required to differentiate between the various infill types. Joint strength is also affected by alteration, so knowledge of alteration analysis is critical. Estimation or averaging of joint parameters can also be a challenge since the influence of a joint set on excavation stability depends on the joint set orientation. It follows that it is advisable to assess joint conditions for individual sets as this permits the use of the most appropriate parameters for the most influential joint set.

Detailed geotechnical log – Log 3

At this stage, an initial estimate of rock strength was obtained using a geological hammer. Rock strength was measured on a scale of R1 to R6, depending on its response to a knock by the hammer (SRK Logging Manual, 2006). R1 signifies highest strength while R6 is for the weakest rock. The geological hammer results were calibrated by sending samples of the rock for laboratory strength tests. The results of the laboratory strength tests are shown in Tables II and III. Table IV gives the results of rock specific gravity measurements from the laboratory tests.

For more accurate results, the authors observed that it is necessary to adopt an evaluation scale for weak rock that quantifies the level of weakness. A scale of S1 to S6 (SRK Logging Manual, 2006) can be used lest detail is lost. It was also observed that intact rock strength (IRS) is affected by elements such as microdefects, foliation, and schistosity, so for representative samples sampling has to be done in multiple orientations. Detailed geotechnical logging was done on a domain basis so as to pick sections of the core with the same geotechnical characteristics. The domains were kept to less than 3 m to preserve accuracy by avoiding overaveraging. In addition to IRS, other parameters evaluated were fracture frequency, joint conditions, cemented joint count, and microfractures.

Overall considerations in geotechnical logging

The geotechnical logging should suit the rock mass classification system to be used. It is imperative for the geotechnical logging sheet to accommodate all the parameters that will be used in the calculation of pillar strength. The logging sheet and instructions should be presented in a way which is easy to understand to minimize human errors and increase accuracy and precision.

Rock characterization from the geotechnical work done at the site

Rock mass classification systems were used to estimate the strength of the rock mass, which is an important parameter for determining pillar strength. The classification systems adopted for the project were the Q-system (Barton *et al.*, 1974), Bieniawski's RMR (Bieniawski, 1989), and Laubscher's MRMR (Laubscher, 1990).



Figure 4–Determination of beta and alpha angles (SRK Logging Manual, 2006)

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Type Diameter Height Bo Density Failure 1553/1 146.50 - 146.16 Type Diameter Diameter g g/cm ³ kN 3753/1 146.50 - 146.70 Gabbro - Norite 47.11 120.9 2.6 605.8 2.87 226.4 153./1 158.54 - 158.69 M2014 158.54 - 158.69 Bronzitite 47.33 114.4 2.4 639.3 3.18 241.1 M2018 159.29 - 159.44 Bronzitite 47.29 118.9 2.5 675.8 3.24 301.7	S BY MEANS OF STRAIN GAUGES S PECIMEN DIMENSIONS S PEC MEN TEST R ample Sample Rock Diameter Height Mass Density Failure S tength No From Type Diameter Height Mass Density Failure S tength 1753/L 146.00-146.16 Type Mass Diameter g g/cm³ kN MPa 1753/L 146.50-146.70 Gabbro - North 47.12 111.8 2.4 560.6 2.88 388.1 222.6 1753/A 145.54-158.69 Gabbro - North 47.14 20.9 2.6 605.8 2.87 226.4 116.7 102104 158.54-158.69 M2016 158.84-158.99 Bronzitite 47.33 114.4 2.4 639.3 3.24 201.1 148.0 M2018 159.29-159.44 Bronzitite 47.29 118.9 2.5 675.8 3.24 301.7 171.8	S BY MEANS OF STRAIN GAUGES SPECIMEN DIMENSIONS SPECIMEN TEST RESULTS ample Sample Rock Diameter Height Na Density Failure Strength Tangent No From Type Diameter Height Mass Density Failure Strength Tangent 1753/L 146.00-146.16 Type Diameter Diameter g g/cm ³ kN MPa GPa 1753/L 146.00-146.16 Gabbro - Northe 47.12 111.8 2.4 560.6 2.88 388.1 222.6 105.0 1753/L 146.50-146.70 Gabbro - Northe 47.11 120.9 2.6 605.8 2.87 226.4 129.9 116.0 173/D 147.38 144.4 2.4 639.3 3.18 241.1 137.0 100.0 M2014 158.54 158.69 Bronzitite 47.33 114.4 2.4 639.3 3.18 241.1 137.0 100.0 M2016	S BY MEANS OF STRAIN GAUGES SPECIMEN DIMENSIONS SPECIMEN TEST RESULTS ample Sample Rock Diameter Height Mass Pensity Failure Strength Tangent Secant No From Type Diameter Height Mass Pensity Failure Strength Tangent Secant 1753/1 146.00 - 146.16 Type Diameter Diameter g g/cm ³ NN MPa GPa GPa 1753/1 146.00 - 146.16 Gabbro - Northe 47.12 111.8 2.4 560.6 2.88 388.1 222.6 105.0 107.0 173.00 147.38 - 147.61 47.11 120.9 2.6 605.8 2.87 226.4 129.9 116.0 103.0 173.00 147.38 - 147.61 47.33 114.4 2.4 639.3 3.18 241.1 137.0 100.0 107.0 173.00 158.84 - 158.69 Brozitite 47.33 114.4 2.4 639.3	S BY MEANS OF STRAIN GAUGES SPECIMEN DIMENSIONS SPECIMEN TEST RESULTS ample Sample Rock Diameter Height Summeter Load Strength Tangent Secant Poisson's No From Type Diameter Height Mass Density Failure Strength Tangent Secant Poisson's 1753/1 146.00-146.16 mm mm mm g g/cm³ kN MPa GPa GPa 1753/1 146.50-146.70 Gabbro - Northe 47.12 111.8 2.4 560.6 2.88 388.1 222.6 105.0 107.0 0.21 173.00 147.38 147.11 120.9 2.6 605.8 2.87 226.4 129.9 116.0 103.0 0.34 173.00 147.38 144.4 2.4 639.3 3.18 241.1 137.0 100.0 107.0 0.31 M2014 158.84 158.99 M27.3 114.4 2.4	S BY MEANS OF STRAIN GAUGES SPECIMEN DIMENSIONS SPECIMEN TEST RESULTS Secant (UCS) Poisson's Ratio Ratio Ratio Poisson's Ratio Poisson's Ratio Tangent to the secant to the secant to the secant to the secant (the secand to the secant	S BY MEANS OF STRAIN GAUGES SPECIMEN DIMENSIONS SPECIMEN TEST RESULTS Poisson's Poisson's Ratio Axial ample Sample Rock Diameter Height No Partic ULARS SPECIMEN DIMENSIONS SPECIMEN TEST RESULTS View Poisson's Poisson's Ratio Strain at to	S BY MEANS OF STRAIN GAUGES SPECIMEN DIMENSIONS SPECIMEN TEST RESULTS Secant Poisson's Ratio Rati Ratio Rati Ratio Rati Ratio Ratio Ratio Ratio Rati Rati Ratio

Note: All tests were conducted according to the ISRM's specifications.

Table	e ///																	
Res	ults of	triaxial co	ompressiv	ve strei	ngth t	ests												
RESULT	SOFTRIA	XIAL COMPR	ESSIVE STRE	NGTHTE	STS WIT	HELAS	LIC MOD	ULUS A	ND									_
POISSON	S RATIO	ME AS URE ME	ENTS BY MEA	NS OF ST	RAIN GA	AUGES												
SPECIM	EN PARTIC	ULARS		SPECIME	N DIMEN:	SIONS				SPECIM	EN TEST F	ESULTS						
Rocklab	Sample	Sample	Rock	Diameter Height Ratio of Mass Density Cor				Confining	Failure	Strength	Tangent	Secant	Tangent	Secant	Linear	Failure	Not	
Specimen						Height			Pressure	Load	(TCS)	Elastic	Elastic	Poisson's	Poisson's	Axial		
No	No.	Depth	Type			to			σ_3	P	σ_1	Modulus	Modulus	Ratio	Ratio	Strain	Code	
		From To				Diameter						@ 50% TCS	@ 50% TCS	@ 50% TCS	@ 50% TCS	at Failure		
3569-		(m)		mm	mm		g	g/cm3	MPa	kN	MPa	GPa	GPa			mm/mm		
TCM-01A	GT53/2	146.16 - 146.33		47.09	99.2	2.1	499.6	2.89	10	475.7	273.1	99.1	101.0	0.34	0.27	0.002790	XA	
TCM-01B	GT53/3	146.33 - 146.5		47.12	98.0	2.1	491.8	2.88	20	608.1	348.7	89.8	102.0	0.30	0.33	0.003977	XA	
TCM-01C	GT53/5	146.70 - 146.85		47.11	96.6	2.1	478.9	2.84	30	394.1	226.1	97.9	126.0	0.18	0.23	0.002138	XA	
TCM-01D	GT53/6	146.85 - 146.93	Gabbro - Norite	47.12	94.3	2.0	467.7	2.84	40	555.1	318.3	93.4	103.0	0.30	0.33	0.003067	8B	
TCM-01E	GT53/7	146.93 - 147.08	Gabbio - Norke	47.12	100.1	2.1	495.6	2.84	10	489.7	280.8	89.2	100.0	0.33	0.28	0.003681	6B	
TCM-01F	GT53/8	147.08 - 147.23		47.12	101.0	2.1	496.9	2.82	20	584.5	335.2	89.7	105.0	0.31	0.34	0.003607	XA	
TCM-01G	GT53/9	147.23 - 147.38		47.12	97.7	2.1	480.2	2.82	30	591.9	339.4	87.4	92.1	0.31	0.29	0.003847	-4B	
TCM-01H	GT53/10	147.38 - 147.61		47.14	93.5	2.0	458.0	2.81	40	625.7	358.5	90.7	94.5	0.34	0.32	0.003469	3B	
TCM-02A	TM2007	157.49 - 157.64		47.29	99.8	2.1	570.0	3.25	10	315.4	179.6	87.3	97.0	0.27	0.26	0.002244	XA	
TCM-02B	TM2008	157.64 - 157.79		47.30	97.6	2.1	548.1	3.19	20	402.9	229.3	85.8	104.0	0.31	0.37	0.002436	XA	
TCM-02C	TM2009	157.79 - 157.94		47.30	94.9	2.0	526.3	3.16	30	328.0	186.7	74.3	89.6	0.25	0.27	0.002953	XA	
TCM-02D	TM2010	157.94 - 158.09	Bronzitite	47.27	98.3	2.1	540.2	3.13	40	357.3	203.6	72.6	88.7	0.26	0.32	0.003662	XA	
TCM-02E	TM2011	158.09 - 158.24		47.30	97.8	2.1	541.4	3.15	10	261.0	148.5	87.3	107.0	0.32	0.40	0.001569	XA	
TCM-02F	TM2012	158.24 - 158.39		47.29	100.8	2.1	560.6	3.17	20	291.2	165.8	89.1	101.0	0.25	0.26	0.001807	XA	
TCM-02G	TM2015	158.69 - 158.84		47.30	94.9	2.0	526.7	3.16	30	366.2	208.4	74.7	90.9	0.26	0.30	0.003648	XA	
TCM-02H	TM2017	158.99 - 159.14		47.29	99.8	2.1	566.5	3.23	40	469.1	267.1	92.5	119.0	0.24	0.27	0.002691	XA	
							,											1

Note: All tests were conducted according to the ISRM's Specification. TCS - stands for Triaxial Compressive Strength.

Table IV

Results of rock specific gravity measurements

	Spicemen pa	articulars			Specific gravity	y measurements		
Rocklab	Sample	Borehole	Rock	Mass	Water	Volume	Bulk	Note
specimen	No	depth	type	after	relative	of the	specific	
No. 3569-		from to m		OD 105°c gram	density g/cc	material cm ³	gravity g/cc	
SG-01	GT 53/1	146.00–146.16		49.29	0.998	17.1	2.870	
SG-03	GT 53/3	146.33-146.5		69.89	0.997	24.3	2.864	
SG-05	GT 53/5	146.70-146.85	Norite	66.33	0.997	23.1	2.864	
SG-07	GT 53/7	146.93-147.08		63.99	0.998	22.4	2.851	
SG-09	GT 53/9	147.23–147.38		66.75	0.998	23.8	2.803	
SG-11	GT 53/11	149.45-149.57		51.01	0.998	16.2	3.141	
SG-13	GT 53/13	149.69–149.81	Websterite	80.09	0.997	25.3	3.160	
SG-15	GT 53/15	149.93-150.05		49.37	0.998	15.3	3.225	
SG-17	TM 2007	157.49-157.64		37.95	0.998	11.8	3.207	
SG-20	TM 2010	157.94-158.09		54.57	0.998	17.3	3.148	
SG-23	TM 2013	158.39-158.54	Bronzitite	39.51	0.998	12.5	3.160	
SG-26	TM 2016	158.84-158.99		49.76	0.998	15.5	3.196	
SG-29	TM 2019	159.29–159.44		69.88	0.997	21.8	3.200	

Link between RMR and Q-system

To compare the Bieniawski RMR and the calculated RMR, transformation Equations [20] and [21] were used.

$$RMR = 9lnQ + 44$$
 (Bieniawski, 1976) [20]

RMR = 5lnQ + 60.8 [21] (South African tunnels - Choquet and Hadjigeorgiou, 1993)

It was noted that results obtained using Equation [20] deviated from the Bieniawski RMR, so Equation [21] was used as it gave a closer correlation. Table IX gives the RMR values calculated from Q using Equation [21]. Table V gives the MRMR classification system results for the project.

Rock mass characterization

For a realistic pillar design criterion, rock mass properties were determined using laboratory uniaxial and triaxial compression tests. The parameters determined were UCS, Poisson's ratio, Young's modulus, and specific gravity. A summary of the tests results is shown in Table VI.

Pillar design considerations

The detailed logging data was processed to give some input into the pillar design at the exploration stage. For calculating strength, design rock mass strength (DRMS) was used instead of the strength of a unit cube of rock. This approach was adopted since DRMS considers all the parameters that

Table V

On-reef zone rock mass classification –

ו) חוזוחוזו	Laubsche)		
Borehole	Zone (m)	RMR	Cumulative adjustments	MRMR
BO 56	45–53	59		40
IBO 01	114–122	74	Weathering	50
BO55A	119–127	72	96%	49
IBO 02	138–146	69		47
BO 54A	142-150	75		51
IBO 03	171–179	63		43
BO 53A	150–158	70	Induced stress	47
IBO 11	182–190	77	100%	52
BO 052	143–151	69		47
BO 045	158–166	74		50
BO 051	115–123	81		55
BO 58	100–108	85	Joint orientation	58
BO 59	114–122	79	75%	53
BO 60	135–143	74		50
BO 61A	132–140	70		47
BO 62	94–102	72		49
BO 66	101–109	72	Blasting	49
BO 68	120–128	84	94%	57
BO 39	189–197	77		52
BO 41	130–138	57		39

Table VI

Summary of laboratory rock tests results

Rock property	Hanging wall	Mineralized zone
Triaxial Compressive Strength (TCS) MPa	310.1	198.6
Uniaxial Compressive Strength (UCS) MPa	156.4	152.3
Density t/m ³	2.84	3.18
Elastic Modulus GPa	97.6	91.4
Poisson's Ratio	0.31	0.29

were assessed in the logging programme which have a bearing on the pillar strength. In determining DRMS, rock mass strength (RMS) is first calculated using Equation [22] (suggested by Laubscher, 1990).

$$RMS = UCS \times (RMR - R_{UCS})/100$$
[22]

where: RMR is the total of the rock mass rating and R_{UCS} is the uniaxial compressive strength rating determined using Bieniawski's (1989) rock mass rating system table.

To obtain the DRMR needed for calculating pillar strength, the RMS was adjusted for the effects of blasting, weathering, and joint orientation, which were 95%, 96%, and 74% respectively. The Hedley and Grant (1972) power formula was used for calculating pillar strength; however, the strength of a unit cube of rock, originally proposed as input, was replaced by DRMR, which is more representative of pillar experience. The formula used is given in Equation [23].

$$P_{s} = DRMS. \frac{W_{e}^{0.5}}{H^{0.7}}$$
 [23]

where DRMS is the design rock mass strength; W_e is the effective pillar width given by 4 × Pillar area/Pillar perimeter, and *H* is the pillar height.

Since the maximum depth of orebody at the exploration site is less than 300 m, the mine to be established is considered to be shallow so the TAT (Equation [1]) was applied. However, the drawbacks of this theory, as discussed earlier, are still valid and further research work need to be undertaken to account for these shortfalls.

A constant safety factor (SF) of 1.6 was used for comparative analysis of the pillar strength formulae at different depth. A SF of 1.6 was used since it is the common SF for non-yielding pillars in South Africa. For calculating the square pillar width at different depths for a constant SF of 1.6, the following values were used in the SF equation (SF = Pillar strength/Pillar load):

Mining height	1.8 m
Pillar centres	18 m
Rock density	2 700 kg/m ³
UCS of intact pillar rock	152.3 MPa
DRMS	48.4 MPa

The resultant square pillar widths at various depths for a constant SF of 1.6 are given in Table VII.

Note that the same approach was adopted to determine pillar width at different depths for a constant SF of 1.6 for different hard-rock pillar design formulae presented in this paper as applied to the project database. This was done to illustrate the uncertainty brought about by these formulae in the pillar design process. The results are as presented in Table X.

The rock mass classification data used for this research is presented in Tables VIII and IX.

Pillar design results using different hard-rock pillar design formulae

To highlight the current uncertainty in the pillar design process, the hard-rock pillar design formulae presented in this paper were used to determine square pillar sizes at different depth using the platinum exploration data. A constant SF of 1.6 was used in the calculations since it is the minimum permitted for the project. The TAT was used to determine the stresses at different depths since the mining layout is of large lateral extent, several times greater than the mining depth, and regular with same-size pillars. It is important to note that the Coates' method reduces to the usual TAT under these conditions (large width of extraction span, L) so only the TAT was used for the assessment.

Since there is no straightforward way of calculating pillar width from the SF equation, several iterations were performed in Excel® to find the pillar width corresponding to

Table VII

Variation of square pillar width with depth at a constant SF of 1.6

Depth below surface (m)	Pillar width (m)	SF
100	4.53	1.6
120	4.88	1.6
140	5.19	1.6
160	5.47	1.6
180	5.73	1.6
200	5.98	1.6

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Table VIII

On-reef zone rock mass classification - Q system (Barton)

	Joint condition													
Borehole	Zone	RQD	Set No.	Roughness	Alteration	Water reduction	Stress reduction	RQD/J _n	J_r/J_a	J _w /SRF	Q			
	(m)		(J _n)	No. (J _r)	No. (J _a)	fact. (J _w)	fact. (SRF)							
BO 56	45–53	76	3	1.5	6	1	2.5	25.3	0.25	0.4	2.5			
IBO 01	114–122	98	3	1.5	1.5	1	2.5	32.7	1	0.4	13.1			
BO 55A	119-127	99	4	1	0.75	1	2.5	24.8	1.3	0.4	12.9			
IBO 02	138–146	89	4	3	3	1	2.5	22.3	1	0.4	8.9			
BO 54A	142-150	98	4	1	1	1	2.5	24.5	1	0.4	9.8			
IBO 03	171–179	57	9	3	1	1	2.5	6.3	3	0.4	7.6			
BO 53A	150-158	100	4	1	1	1	2.5	25.0	1	0.4	6.3			
IBO 11	182-190	100	2	1.5	0.75	1	2.5	50.0	2	0.4	40.0			
BO 52	143–151	75	9	3	1	1	2.5	8.3	3	0.4	10.0			
BO 45	158-166	96	3	1.5	0.75	1	2.5	32.1	2	0.4	25.7			
BO 51	115-123	99	4	3	1	1	2.5	24.8	3	0.4	29.7			
BO 58	100-108	100	1	1	1	1	2.5	100.0	1	0.4	40.0			
BO 59	114–122	95	4	3	2	1	2.5	23.8	1.5	0.4	14.3			
BO 60	135–143	96	6	1.5	1	1	2.5	16.0	1.5	0.4	9.6			
BO 61A	132-140	99	6	1	1	1	2.5	16.5	1	0.4	6.6			
BO 62	94–102	95	9	1.5	1	1	2.5	10.6	1.5	0.4	6.4			
BO 66	101-109	100	4	1	1	1	2.5	25.0	1	0.4	10.0			
BO 68	120-128	100	1	1	1	1	2.5	100.0	1	0.4	40.0			
BO 39	189–197	98	2	1.5	1	1	2.5	49.0	1.5	0.4	29.4			
BO 41	130–138	77	15	4	4	1	2.5	5.1	1	0.4	2.0			

Table IX									
On-reef z	one rock	mass cla	assifica	tion – RMR (Bieniawski)				
Borehole	Zone (m)	RQD	UCS	Joint spacing	Joint condition	Ground water	Joint orientation	RMR	Calculated RMR from Q*
BO 56	45–53	17	12	8	12	15	-5	59	65
IBO 01	114–122	20	12	10	22	15	-5	74	74
BO 55A	119-127	20	12	10	20	15	-5	72	74
IBO 02	138–146	17	12	10	20	15	-5	69	72
BO 54A	142-150	20	12	15	18	15	-5	75	72
IBO 03	171–179	13	12	8	20	15	-5	63	71
BO 53A	150-158	20	12	10	18	15	-5	70	70
IBO 11	182-190	20	12	15	20	15	-5	77	79
BO 52	143–151	17	12	8	22	15	-5	69	72
BO 45	158–166	20	12	10	22	15	-5	74	77
BO 51	115-123	20	12	15	24	15	-5	81	78
BO 58	100-108	20	12	20	23	15	-5	85	79
BO 59	114–122	20	12	15	22	15	-5	79	74
BO 60	135–143	20	12	10	22	15	-5	74	72
BO 61A	132–140	20	12	10	18	15	-5	70	70
BO 62	94-102	20	12	10	20	15	-5	72	70
BO 66	101-109	20	12	10	20	15	-5	72	69
BO 68	120-128	20	12	20	22	15	-5	84	79
BO 39	189–197	20	12	15	20	15	-5	77	78
BO 41	130–138	17	12	8	10	15	-5	57	64
*RMR=5InQ	+ 60.8			·					·

a SF of 1.6 for each pillar strength formula. For the sake of clarity and brevity, the formulae presented earlier are not repeated here, but the values of the parameters as applied to the platinum exploration database are given and the results summarized in Table X. The parameters used in the pillar design exercise are as follows: mining height 1.8 m, pillar centres 18 m, rock density 2 700 kg/m³, UCS of intact pillar rock 152.3 MPa, and DRMS 48.4 MPa. The other parameter values for each of the formulae are as presented in Table I. The results of the pillar design exercise are summarized in Table X.

Comments on pillar design results from the different design formulae

After exploration is completed one needs a clear method for

designing pillars to ensure a reliable, safe, and stable design. One is faced with an arduous task of choosing which formulae to use as the different formulae all give different pillar sizes at constant mining depth. The results show that there is no clear way of solving the pillar design problem. This points to a need for further research dedicated to resolving this problem. All the relevant factors influencing pillar design have to be considered and combined into an effective procedure or formula that pillar design practitioners for narrow-reef platinum mining can use.

The evaluation concluded that the current pillar design systems for narrow-reef platinum mining mainly consider w/h ratio and the strength of pillar material as important parameters in designing pillars. However, there are many more important factors that are not considered which have a

Table X

Pillar design results for the different pillar design formulae

ath Ctuo					
a) (I	ss (TAT) MPa)	Depth (m)	Pillar width (m)	w/h ratio	SF
71 9	3 43	100	3.06	1 70	16
20 5	2 55	100	4.08	2 27	1.0
11 3	1.50	100	5.27	2.93	1.0
14 7	4 79	100	3.4	1.90	1.6
27 4	2.63	100	4 53	2.52	1.6
20 5	7.81	100	3.89	2 16	1.0
75 6	0.26	100	3.81	2.12	1.6
24 9	6.98	120	3.29	1.83	1.6
18 5	4.22	120	4.40	2.44	1.6
19 3	2.54	120	5.68	3.16	1.6
33 7	9.67	120	3.63	2.02	1.6
35 4	4.08	120	4.88	2.71	1.6
71 5	9.51	120	4.20	2.33	1.6
01 6	2.45	120	4.10	2.28	1.6
11 9	9.98	140	3.50	1.94	1.6
59 5	5.92	140	4.68	2.60	1.6
75 3	3.57	140	6.04	3.36	1.6
52 8	3.93	140	3.82	2.12	1.6
07 4	5.47	140	5.19	2.88	1.6
15 6	1.29	140	4.47	2.48	1.6
60 6	3.84	140	4.38	2.43	1.6
63 10	2.24	160	3.70	2.06	1.6
95 5	7.36	160	4.94	2.74	1.6
22 3	4.39	160	6.38	3.54	1.6
36 8	7.48	160	4.00	2.22	1.6
02 4	6.78	160	5.47	3.04	1.6
50 6	2.56	160	4.73	2.63	1.6
38 6	5.29	160	4.63	2.57	1.6
37 10	5.14	180	3.87	2.15	1.6
98 5	8.68	180	5.18	2.88	1.6
51 3	5.29	180	6.68	3.71	1.6
50 9	0.99	180	4.16	2.31	1.6
78 4	7.96	180	5.73	3.18	1.6
6 6	4.01	180	4.96	2.76	1.6
/5 6	6.67	180	4.86	2.70	1.6
02 10	7.20	200	4.04	2.24	1.6
37 5	9.78	200	5.41	3.01	1.6
77 3	6.01	200	6.97	3.87	1.6
43 9	4.62	200	4.30	2.39	1.6
43 4	8.93	200	5.98	3.32	1.6
	5.20	200	5.18	2.88	1.6
1 6	7.53	200	5.09	2.83	1.6
	iggin Street iggin Street iggin (I) 71 9 20 5 41 3 44 7 27 4 90 5 75 6 24 9 18 5 19 3 83 7 85 4 71 5 01 6 11 9 69 5 75 3 52 8 07 4 15 6 60 6 611 9 52 3 86 8 02 4 50 6 37 10 98 5 51 3 50 9 78 4 58 6	Iggin Stress (TAT) 'a) (MPa) 71 93.43 20 52.55 41 31.50 44 74.79 27 42.63 90 57.81 75 60.26 24 96.98 18 54.22 19 32.54 83 79.67 85 44.08 71 99.98 69 55.92 75 63.57 11 99.98 69 55.92 75 33.57 52 83.93 07 45.47 15 61.29 60 63.84 63 102.24 95 57.36 22 34.39 86 87.48 02 46.78 50 62.56 88 65.29 37 105.14 98 58.68<	Stress (1A1) Depth (m) (m) 71 93.43 100 20 52.55 100 41 31.50 100 44 74.79 100 27 42.63 100 90 57.81 100 75 60.26 100 24 96.98 120 18 54.22 120 19 32.54 120 83 79.67 120 85 44.08 120 71 59.51 120 01 62.45 120 11 99.98 140 69 55.92 140 60 63.84 140 63 102.24 160 95 57.36 160 22 34.39 160 63 102.24 160 64 87.48 160 02 46.78 160	rightStress (IA1)DepthPillar width Pa)(MPa)(m)(m)7193.431003.062052.551004.084131.501005.274474.791003.42742.631004.539057.811003.897560.261003.812496.981203.291854.221204.401932.541205.688379.671203.638544.081204.887159.511204.100162.451204.101199.981403.506955.921404.687533.571406.045283.931403.820745.471405.191561.291404.476063.841404.3863102.241603.709557.361604.6337105.141803.879858.681805.185135.291806.685090.991804.167847.961805.738865.291604.635135.291806.685090.991804.167847.961805.73	Stress (IA1) Deptn Pillar width w/n ratio va (MPa) (m) (m) w/n ratio 71 93.43 100 3.06 1.70 20 52.55 100 4.08 2.27 44 74.79 100 3.4 1.90 27 42.63 100 4.53 2.52 90 57.81 100 3.89 2.16 75 60.26 100 3.81 2.12 24 96.98 120 3.29 1.83 18 54.22 120 4.40 2.44 19 32.54 120 3.63 2.02 85 44.08 120 4.88 2.71 71 59.51 120 4.20 2.33 01 62.45 120 4.10 2.28 11 99.98 140 3.50 1.94 69 55.92 140 4.68 2.60 <tr< td=""></tr<>

bearing on pillar system stability. Some of the unaccountedfor factors that were discovered during the course of this research are contact of the pillar with the roof and floor, roof and floor conditions (Watson, 2010), effects of adversely oriented joints, spalling and side scaling effects, influence of pillar loading conditions, blast damage effects, influence of weak layers and weathering, impact of k-ratio, timedependent effects, geology, fractured zones, and effects of different types of discontinuities within the rock strata.

Conclusions

A reliable pillar design system results in a layout with the desired stability. The main objective of this research was to critically evaluate the current pillar design systems used in narrow-reef platinum mining using practical experience from a large feasibility-stage platinum exploration project. The shortcomings of the current pillar design systems were highlighted. The exploration work also highlighted how rock mass classification methods can be utilized in determining

the overall strength of pillars. Geotechnical parameters important for pillar design were collected by means of geotechnical logging and laboratory tests. The geotechnical logging consisted of three stages: quick log per run, major structures log, and detailed geotechnical log. Areas that require special attention in each logging stage were highlighted. It is imperative for the geotechnical logging sheet to accommodate all the parameters that will be used in the calculation of pillar strength. The logging sheet and instructions should be presented in a way that is easy to understand to minimize human errors and increase accuracy. It suffices to say that the quality of input into the pillar design system influences the quality of the results obtained.

Pillar design results using different hard-rock pillar design formulae were significantly different, showing the uncertainty introduced by the current pillar design formulae in the pillar design process. These results show that there is currently no clear way of solving the pillar design problem. Further research has to be dedicated to resolving this challenge

- Reliable pillar design systems depend on the accurate > determination of pillar load and pillar strength. There are many factors influencing these two variables that are unaccounted for in the current pillar design systems. The current systems consider pillar material strength and *w/h* ratio in determining pillar strength, but the failure of even high safety factor pillars is an indication of the overestimation of pillar strength because other determining factors are omitted, such as contact of the pillar with the roof and floor, roof and floor conditions, effects of adversely oriented joints, spalling and side scaling effects, influence of pillar loading condition, blast damage effects, influence of weak layers and weathering, impact of k-ratio, timedependent effects, geology, fractured zones, and effects of different types of discontinuities within the rock strata
- The tributary area theory works well for shallow mining when the pillar layout is regular. The theory assumes that each pillar in the system carries an equal amount of load in the layout; however, pillars near permanent abutments carry less load. It is imperative to note that mining potholes and fault losses, often left out in practical mining, reduce extraction ratios, which in turn results in a lower APS than what is planned for
- ➤ The current pillar design systems for narrow-reef platinum mining were empirically developed and require pillar failure to occur in order to calibrate the pillar design empirical curves. This approach works for the design of pillars in areas lying within the empirical range used to develop the curves. However, some pillars designed this way and which meet the definition of the empirical database nevertheless fail, showing that more parameters need to be considered in the empirical database when deriving the formulae.

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